

# Adversaries with Limited Information in the Friedkin-Johnsen Model

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February 20, 2023

# Malicious Actors are Attacking Social Networks



(The New York Times, 2016)

- 2016 Democratic National Committee email leak.
  - *Russian military and intelligence services have been using the Internet to sow discord and discredit legitimate political institutions* (TIME, 2016)

# Malicious Actors are Attacking Social Networks

## Iranian regime 'doubling down' on media manipulation in response to recent protests, analysis shows

by University of Exeter

(Phys.org, 2022)

### ■ Mahsa Amini protests.

- A recent analysis regarding the Iranian disinformation shows the main goal is to **pit groups against each other.** (The Washington Institute, 2022)

# How Much Discord Can Attackers Sow on Social Networks, Given Limited Information?

# How Do People Form Opinions

Friedkin-Johnsen Model (FJ model) (Friedkin, Johnsen; 1990)

- Each node  $i$  has **innate** and **expressed** opinions
- **Innate** opinion  $s_i \in [0, 1]$ : fixed, kept private
- **Expressed** opinion  $z_i^t \in [0, 1]$ : depends on time  $t$ , public

After convergence  $\mathbf{z} = (I + L)^{-1}\mathbf{s}$ , where  $L$  is the graph Laplacian.

- **Expressed** opinions  $\mathbf{z}$  are determined by the **network topology** and **innate** opinions.

# How to Use Opinions to Measure Societal Discord

In the literature, people use **polarization** and **disagreement** to indicate societal discord.

- Both **polarization** and **disagreement** can be measured by **expressed** opinions.
  - **Polarization**: Variance of **expressed** opinions;
  - **Disagreement**: Tension of **expressed** opinions between neighbors.
- **Expressed** opinions are determined by **network topology** and **innate** opinions.
- $\Rightarrow$  **polarization** and **disagreement** are determined by **innate** opinions and **network topology**.

# Assumptions

- The adversary can *only* access the **network topology**;
  - It is expensive for adversaries to obtain **innate** opinions
  - **Network topology** is accessible, e.g., by data crawling or and API.
  - Previous literature assumes both **innate** opinions and **network topology** are known.
- Small number of network users can be **radicalized**.
  - For Covid vaccination, the attacker may spread disinformation to make some net users to question its safety.
  - **Strong assumption:** The chosen users' opinions can be radicalized.

# Problem Definition



# Maximize discord with Limited Information

## Problem (Full-information)

*Given a social network's topology and its users' **innate** opinions, maximize the discord by radicalizing innate opinions of  $k$  users.*

## Problem (Limited-information)

*Given a social network's topology, maximize the discord by radicalizing innate opinions of  $k$  users.*

- We solve the problem under the limited-information setting.
- We compare our solutions with solutions obtained under full-information setting.

# Our Results

# Theoretical Contributions

- Algorithms that work well under the limited-information setting, also work well under full-information setting.
  - Under mild assumptions, i.e., the network initially has small discord.
- We propose an algorithm with provable guarantee under the limited-information setting.
- We show the hardness of an open problem under both settings.

# Experimental Results

Regarding maximizing **disagreement**.

- The limited information algorithms outperform the baseline algorithms.
- Algorithms using limited information are within a factor of 2 compared to algorithms with full information.

# Ethical Issues

# Datasets

- Public datasets [Twitter](#) and [Reddit](#) have been used in various research papers.
  - [Twitter](#) contains ground-truth opinions.
  - [Reddit](#) contain synthetic opinoins generated using a power law distribution.
- [karate](#), [books](#), [blogs](#) are obtained from public data repository KONECT.
  - The datasets only contain network structure.
- The following datasets appeared in multiple published research papers. However, these datasets are not in the public domain.
  - Tweet:S5, Tweet:S2, Tweet:M5, G:Brexit, G:US-elect and Twitter100.

# Ethical Reflection

- Our work investigates the power of a weak adversary and raises awareness to potential adversarial manipulations.
  - The adversary can sow great discord in the network given only network topology.
  - A simple, common, and scalable greedy algorithm works well for adversaries.
- Ways to mitigate the influence from adversaries:
  - Make attackers hard to obtain **network topology**.
  - Protect its users from adversary who tries to change their opinions.
    - ▶ Protect its users from dis- and mis-information.

Thank You